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The statistical tables, questions and answers, video links as well as SPSS and CSV versions of the data files from the print book are available for download from the book's web page (www.wiley.com/go/walters/medicalstatistics).